



Methodological Starting Points

- The analysis should be a *conceptual* analysis or a formal construction of some important conceptual features of information flow (or some concept thereof).
- It is based on principles deemed to be correct. The set of them might be incomplete.
- It is not an analysis and reconstruction of our present day intuitions.

Study of Logic, Language, and

Study of



UNIVERSITAT

Manuel Bremer, Daniel Cohnitz Information Flow and Situation Semantics **ESSLLI 2002**

Methodological Starting Points (II) • Examples show modelling real information flow (IF) requires many disciplines (logic, cognitive sciences, sociology...). A model of IF in its own terms tries to arrive at (abstract) laws of information flow. • The model in its generality covers both physical systems and mathematical proofs! Centre for th HEINRICH HEINE

Manuel Bremer, Daniel Cohnitz Information Flow and Situation Semantics ESSLLI 2002

Distributed Systems • IF depends on relationships in *a distributed* system (e.g., a telephone connection). • *How* the system is carved up is part of the model of the IF to be explained. • The parts of a distributed system are related to each other by the system as a whole. • Regularities ensure the uniform behaviour of the system. – Has it to be deterministic? Manuel Bremer, Daniel Cohnitz Study of HEINRICH HEINE Logic, Information Flow and Situation Semantics UNIVERSITA anguage, and **ESSLLI 2002** DISSELDOR Information







Information Flow and Causality • IF is required to be reliable. That doesn't mean that is –as might be *reliability*– can be analysed using the concept of causality. • The direction of IF is not necessarily aligned with the direction of causation. Informational dependence isn't causal. • In case of loose connections a causal connection might be not sufficient for IF. Manuel Bremer, Daniel Cohnitz Study of HEINRICH HEINE Logic, Information Flow and Situation Semantics UNIVERSITA Language, and

Information

DISSELDOR

ESSLLI 2002















Information Channels (Outline)

- In the outline we said that information flows in a distributed system. The system can be considered an *information channel*.
- We also said that IF involves the reliable regularities/constraints that connect parts of the system with each other *via* the system.
- This requires mappings from parts to the system as a whole, called "infomorphisms".

Centre for the Study of Logic, Language, and Information

HEINRICH HEINE

UNIVERSITA

DESSELDOR

UNIVERSITAT



Manuel Bremer, Daniel Cohnitz Information Flow and Situation Semantics ESSLLI 2002

Manuel Bremer, Daniel Cohnitz

FSSLLL 2002

Information Flow and Situation Semantics





Infomorphism Example

- We are mainly interested in infomorphism that map parts (e.g. a switch) to the whole system (e.g. a circuit with a bulb).
- The classification concerning switches has a set of switches as objects and types that apply to switches. The classification of the whole distributed system contains switches *build into a circuit* and types *of these*.



Centre for th

Language, and

Information

Study of

Logic,

Manuel Bremer, Daniel Cohnitz Information Flow and Situation Semantics ESSLI 2002

Infomorphism Example (II) • If in our theory of (isolated) switches we have "a pressed switch shows red top", in our theory of flashlights (with switches) we have "in a flashlight a pressed switch shows red top". Consider now a switch build in. • Expressed with the fundamental property: the switch shows red top \Leftrightarrow the flashlight has red top shown $f^{\mathbf{v}}(\mathbf{c}) \mid =_{\mathbf{A}}$ $f^{(\alpha)}$ Centre for th HEINRICH HEINE Manuel Bremer, Daniel Cohnitz Study of Information Flow and Situation Semantics UNIVERSITAT ESSLLI 2002





Regularities at System Level (II) • The classification of switches A₁ contains a type *Pressed*, the classification of bulbs A₂ contains a type On, but they are not related. • On the system level there are types corresponding to Pressed (say Pressed_f) and to On (say $On_{\rm f}$) which at the system level C are connected by constraints: $Pressed_{f} \mid -_{C} On_{f}$ (If a flashlight with pressed button has a bulb that is on, for example) Centre for th Manuel Bremer, Daniel Cohnitz Study of HEINRICH HEINE Logic, Information Flow and Situation Semantics UNIVERSITÄ Language, and

DEISSELDORI

Information

ESSLLI 2002



Connected Tokens

• Two parts (tokens of constituent classifications) are *connected* if the same token of the co-domain is mapped onto them.

• Example:

A switch s is connected to a bulb b if the infomorphism between the switch classification and the system classification, resp. the co-domain (i.e. the domain of flashlights) maps some flashlight token c to the switch s and the infomorphism between the bulb classification and the system classification maps the very same flashlight c to the bulb b. s and b, therefore, are the switch and bulb of the same flashlight. Information only flows in the context of a particular token of the co-domain

Centre for the Study of Logic, Language, and Information



Manuel Bremer, Daniel Cohnitz Information Flow and Situation Semantics ESSLI 2002

Information Flow (Outline)

Suppose A and B are constituent/part classifications in an information channel with core C. A token a of type α in A carries the information that a token b is of type δ in B relative to the channel *C* if a and b are connected in C and the translation of α entails the translation of δ in Th(C).

Centre for the Study of Logic, Language, and







Information Flow and Situation Semantics ESSLLI 2002









f-Intro and *f*-Elim (Use)

- The validity preserving nature of the *f*-Intro rule tells us that any constraint that holds for a constituent of a system translates to a constraint that holds for the system.
- And using *f*-Elim we have that any constraint about the whole system gives a constraint about the components (i.e. those components that are part of a system token).

HEINRICH HEINE UNIVERSITAT DUSSELDORF

Study of

Language, and

Information

Logic,

Manuel Bremer, Daniel Cohnitz Information Flow and Situation Semantics ESSLI 2002







Moving Around Local Logics

• Given an informorphism between A and C and a logic L on one we obtain a natural logic on the other. If L is a logic on A, f[L]is the logic on C obtained from L by f-Intro, $f^{-1}[L]$ is the logic on A obtained from a logic L on C by f-Elim. ("Log_C(A)" an induced logic) • Reasoning at a distance in our diagram is: $Log_{C}(B) = f^{-1}[f[Log(A)]]$

Centre for th Study of Logic, Language, and Information

HEINRICH HEINE

UNIVERSITAT

DIISSELDORI



Manuel Bremer, Daniel Cohnitz

ESSLLI 2002

Information Flow and Situation Semantics

How Information Really Flows (Example)

Let C be again our flashlight classification, B and S be the bulb and switch classifications. We build a classification B+S and an informorphism $f=f_1+f_2$, so that for a flashlight token c $f^{\bullet}(c)=(f_1^{\bullet}(c), f^{\bullet}_2(c))$ are the bulb and switch of c. Given a type ϕ of C $f^{-1}(\phi)$ is the disjoint union of $f_1^{-1}(\phi)$ and $f_2^{-1}(\phi)$. If B supports the constraint LIT $|-_B$ LIVE, this will be a constraint of B+S. Then by *f*-Intro we have a constraint $f(LIT) |-_F f(LIVE)$. Now F supports ILLUM $|-_F$ ELEC (say emitting photons entails carrying current). We might have ILLUM=f(LIT)= $f_1(LIT)$, and ELEC= $f(PRESS)=f_2(PRESS)$. With *f*-Elim we get LIT $|-_{B+S}$ PRESS (i.e. we know that the switch is pressed, since the bulb is lit) – what only holds for pairs that are connected by the same flashlight, these being the *normal* tokens of the logic obtained by applying *f*-Elim, i.e. $Log_C(B+S) = f^{-1}[L]$ for the local logic *L* on C.

Centre for the Study of Logic, Language, and Information



Manuel Bremer, Daniel Cohnitz Information Flow and Situation Semantics ESSLLI 2002